Non-linear evolution and acceleration of unstable fuel-lean hydrogen/air flame at ambient and cryogenic temperatures

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Abstract

Hydrogen storage at cryogenic temperatures is crucial for industrial applications, yet these conditions can significantly affect flame behavior. Both Darrieus-Landau instability (DLI) and diffusional-thermal instability (DTI) can intensify at cryogenic temperature, leading to unique flame dynamics relevant to safe hydrogen usage. In this study, two-dimensional simulations are performed to assess the effects of cryogenic temperature on the non-linear evolution and acceleration of fuel-lean hydrogen/air flames. By changing the initial temperature and equivalence ratio of the unburned gas as well as the channel width, distinct flame evolution regimes driven by the interplay of DLI and DTI are identified. Specifically, for fuel-lean hydrogen/air flames, the growth rate of DLI and DTI in the linear stage increases at cryogenic temperatures. In the non-linear stage, DTI leads to the chaotic evolution of the cellular flame, which is further destabilized at cryogenic temperatures. It is found that the long-term dynamics, characterized by cell splitting, merging, and lateral movement, result from complex interactions among flow, flame stretch, and chemical reactions. Moreover, flame structure analysis shows that, compared to ambient temperatures, cryogenic temperatures significantly increase the local reaction rate. The propagation speed of fuel-lean

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hydrogen/air flames is further accelerated at cryogenic temperature, which is associated with the combined effects of enhanced local reaction rate and increased flame surface area, with the primary contribution from enhanced DTI and the secondary contribution from enhanced DLI. In contrast, stoichiometric and fuel-rich flames propagate in a stable single-cusp shape, with their acceleration primarily driven by DLI and flame surface area increase. The width of the channel also affects cellular flame evolution. Rather than altering reaction rates, channel geometry influences flame acceleration mainly through constraining the surface area during flame propagation. These insights contribute to our understanding of cryogenic hydrogen flame dynamics and have important implications for hydrogen safety management.

Keywords: Hydrogen flame, Cryogenic temperature, Cellular instabilities, Non-linear evolution

Novelty and Significance Statement

The novelty of this study lies in assessing and interpreting the effects of cryogenic temperatures on fuel-lean hydrogen/air flames subjected to both Darrieus-Landau instability (DLI) and diffusional-thermal instability (DTI) for the first time. Through detailed numerical simulations, we reveal mechanisms driving the chaotic evolution and cellular structure of flame fronts under cryogenic conditions. Our quantitative analysis demonstrates the relative contributions of DLI and DTI. The research fills a critical knowledge gap by examining the role of DLI and DTI at cryogenic conditions for highly unstable fuel-lean hydrogen/air flame. The results are especially valuable for predicting and managing potential flame acceleration hazards in cryogenic hydrogen systems, where traditional ambient-temperature models may not adequately capture the underlying physics.

Author Contributions Statement

- L. Yang: Conceptualization, Methodology and formal analysis, Writing original draft, Writing –review & editing
- T. Zhang: Assisted in further analysis, Writing review & editing.
- Y. Wang: Assisted in further analysis, Writing review & editing.

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- Z. Chen: Conceptualization, Methodology, Writing –review & editing, Funding acquisition, Supervision.

1 1. Introduction

Recently, hydrogen has received great attention for its potential to reduce 2 carbon dioxide emissions [1, 2]. Cryogenic storage and hydrogen transporta-3 tion are necessary for some applications due to gaseous hydrogen's low vol-4 umetric energy density. Due to the low minimum ignition energy and high 5 diffusivity and reactivity, safety issues related to cryogenic hydrogen pose 6 a serious problem to hydrogen utilization [3]. After accidental release, liq-7 uid hydrogen can evaporate rapidly and mix with ambient air [4], forming 8 a cryogenic premixed hydrogen/air mixture, leading to possible deflagration 9 after ignition [5]. Moreover, the onset of flame instabilities may lead to 10 the deflagration-to-detonation transition (DDT) through flame acceleration, 11 causing faster energy release and more severe damage [6-8]. Therefore, it is 12 important to understand the propagation and acceleration of hydrogen/air 13 flames subject to instabilities at cryogenic temperatures. 14

In the absence of gravity [9], intrinsic flame front instabilities including 15 Darrieus-Landau instability (DLI, or hydrodynamic instability) and diffusional-16 thermal instability (DTI) [10–13], can greatly accelerate the flame propaga-17 tion through flame front wrinkling. Under cryogenic conditions, the DLI can 18 be enhanced as the expansion ratio (density ratio of unburned to burned 19 gas, i.e., $\sigma = \rho_u / \rho_b$ becomes large [14]. The DTI can also become signifi-20 cant since the Zel'dovich number increases with decreasing temperature for 21 fuel-lean hydrogen/air flames with sub-unity Lewis number (Le < 1) [11, 15]. 22 Previous studies [7, 16, 17] demonstrated that DLI at cryogenic temperatures 23 can be much stronger than that at ambient temperatures for stoichiometric 24 hydrogen/air flame. For turbulent flames, the effect of DLI on flame accel-25 eration was studied by Chen *et al.* [18]. These studies show that a large 26 expansion ratio at cryogenic temperatures causes strong flame acceleration. 27 In the recent work by Missey *et al.* [19], the impact of fuel stratification on 28 the propagation of cryogenic fuel-lean flame above a liquid hydrogen pool 29 was analyzed. They found that flame instabilities play a role in flame ker-30 nel development in the early stage. However, the impact of instabilities on 31 long-term flame propagation and acceleration was not thoroughly discussed. 32 For fuel-lean hydrogen/air flames at cryogenic temperatures, the combined 33 effects of DLI and DTI may lead to even stronger flame acceleration, posing 34 risks to the safe use of hydrogen. In the literature, there is a lack of quantita-35 tive analysis on the effects of DLI and DTI on the evolution and acceleration 36 of cryogenic fuel-lean hydrogen/air flame, which inspires the present study. 37

There are several theoretical studies on linear instabilities development 1 for planar flame [20, 21], circular expanding flame [22], and spherical ex-2 panding flame [23]. However, for fuel-lean hydrogen/air flames, Frouzakis et 3 al. [24] have shown that linear theory fails to predict the dispersion relation. 4 In addition, the non-linear evolution of wrinkled flames is more relevant to 5 practical applications since linear evolution only lasts for a relatively short 6 interval. Although analytical theory [25, 26] on the non-linear evolution of unstable flames has been developed, it cannot be readily applied to cryogenic 8 flame evolution due to the strong assumption of weak thermal expansion. To 9 account for realistic thermal expansion, a modified model in the context of 10 hydrodynamic theory [27, 28] has been developed. However, the modified 11 model requires numerical treatment, and the internal structure of the flame 12 front is greatly simplified. Therefore, numerical research is still needed to 13 study the evolution and acceleration of the fuel-lean hydrogen/air flames at 14 cryogenic temperatures. 15

Various numerical studies in the literature have focused on the evolution 16 of premixed hydrogen/air flames at ambient temperatures [29–34]. Berger et17 al. [15] investigated the effects of pressure, equivalence ratio, and temperature 18 on premixed hydrogen/air flame instabilities in the linear stages. They found 19 that intrinsic instabilities can be enhanced by decreasing the equivalence ratio 20 and the temperature of the unburnt gas or by increasing the pressure. Later 21 on, they studied the non-linear evolution of unstable hydrogen/air flames 22 subjected to instabilities including DLI and DTI [31]. Their results showed 23 that the instability development in the non-linear stage is affected by equiv-24 alence ratio, initial temperature, and pressure in the same manner as that 25 in the linear stage in [15]. A recent study by Attili et al. [35] suggested that 26 pressure can affect the development of DLI through different mechanisms. In 27 addition, the contribution of DLI and DTI, as well as the synergistic interac-28 tion between DLI and DTI on flame evolution, was investigated numerically 29 by Berger *et al.* [36]. However, none of the studies mentioned above covered 30 the cryogenic temperature range. The impact of cryogenic temperatures on 31 fuel-lean hydrogen/air flame evolution and accelerative propagation remains 32 unclear. This motivates the present study, which focuses on the instability 33 development of cryogenic fuel-lean hydrogen/air flames. 34

Given the background mentioned above, this study aims to investigate the fuel-lean hydrogen/air flame propagation subjected to intrinsic instabilities at cryogenic temperatures, focusing on the long-term non-linear evolution and acceleration associated with strong DLI and DTI. The paper is organized as follows. Section 2 provides an overview of the numerical models and details
on the setup. Then, Section 3 presents the simulation results and discusses
various factors affecting the propagation and acceleration of fuel-lean flames.
Finally, Section 4 summarizes the findings of this study.

5 2. Numerical model and methods

We consider premixed hydrogen/air flame propagation in a two-dimensional 6 rectangular channel, as shown in Fig. 1. This configuration has been used to 7 study flame instabilities [24, 29, 36]. The flame propagates from the right end 8 to the left. Periodic boundary conditions are imposed on the top and bot-9 tom of the domain, while inflow and outflow boundary conditions are applied 10 to the left and right boundaries, respectively. Note that periodic boundary 11 conditions, rather than wall boundary conditions, are employed to prevent 12 the flame quenching, which could otherwise affect the development of flame 13 instabilities. 14



Figure 1: Schematic of the computational domain for the planar H_2/air flame propagating towards the left inlet.

¹⁵ We consider factors affecting the flame instabilities, including equivalence ¹⁶ ratio ϕ , initial temperature T_0 , and channel width h. Although the fuel-¹⁷ lean hydrogen/air mixtures with the equivalence ratio of $\phi=0.5$ and initial ¹⁸ temperatures of $T_0 = 100$ K and 300 K are the focus of this study, simulations ¹⁹ with $\phi=1.0$ and $\phi=2.5$ are conducted to evaluate the effect of DLI alone, as ²⁰ shown in Table 1.

The channel width depends on the equivalence ratio and temperature of the mixture. The length of the computational domain is fixed to $L = 100\delta$, where δ is the flame thickness of the corresponding 1D premixed planar flame. It is determined by the maximum temperature gradient, i.e., $\delta = (T_b - T_0)/(dT/dx)_{max}$. Here T_b and T_0 are the temperatures of burned and

cases	$\phi = 0.5$	$\phi = 1$	$\phi = 2.5$
$T_0 = 100 \text{ K}$	DLI&DTI	DLI	weak DLI
$T_0 = 300 \text{ K}$	DLI&DTI	DLI	weak DLI

Table 1: Cases with different initial temperatures (T_0) and equivalence ratios (ϕ) considered in this study.

unburned gases, respectively. Cantera [37] is used to calculate 1D unstretched planar flame parameters, such as laminar flame speed S_L and flame thickness 2 δ. The width of the computational domain varies by case, and a series of 3 values are considered: $h=4\delta$, 5δ , 6δ , 8δ , 10δ , 40δ , and 100δ . According 4 to a previous study [30], for unstable hydrogen/air flames, a large domain 5 $(h > 25\delta)$ is necessary to ensure that the channel width does not constrain the 6 development of instabilities. Note that the flame is stable for channels with $h < 4\delta$, and the flame front remains planar without wrinkling. Therefore, 8 these channel widths, unaffected by flame instabilities, are not considered in 9 the present study. 10

The domain is initialized by the corresponding 1D flame profile, and the 11 flame front is located at $x = 90\delta$. The unburned gas velocity from the inlet 12 is S_L . By imposing small sinusoidal perturbations on the flame front, the 13 flame propagates towards the inlet due to the development of instabilities. 14 As adopted in the previous study [24], here we also take the perturbation 15 amplitude as $A(t = 0) = 0.001\delta$, and the wavelength λ is set to be the 16 channel width $(\lambda = h)$ for different cases. In the following section, unless 17 otherwise specified, the length and time scales are normalized by δ and δ/S_L , 18 respectively. 19

The low-Mach number solver, PeleLM [38], is used to solve the Navier-20 Stokes equations for multi-component reactive flow in the low-Mach number 21 limit. The detailed chemical mechanism developed by Konnov [39] and the 22 mixture-averaged transport model are considered in the simulations. This 23 mechanism was used in previous studies [14, 16] to simulate cryogenic hy-24 drogen/air flame propagation. It is also found that results are insensitive to 25 cryogenic temperatures [40]. The Soret diffusion effect is neglected in the 26 simulations as previous studies |41-43| have shown that it does not lead to 27 qualitative change to hydrogen flames and that its importance appears nearly 28 constant from $T_0 = 300$ K to 100 K [44]. To perform the simulation efficiently, 29 adaptive mesh refinement is employed with a base grid size of $\Delta x = \delta/4$. The 30

¹ reaction front is consistently resolved using a fine grid with a minimum size ² of $\Delta x = \delta/32$ throughout the simulation. This grid is fine enough to resolve ³ the thin flame front and avoid numerical noise [24, 27], which was considered ⁴ to be a major factor that affects the evolution of large-scale flames [45]. Af-⁵ ter a short period of linear evolution, the chaotic evolution in the non-linear ⁶ stage happens, which will be analyzed and discussed in the following section.

7 3. Results and discussion

$_{\rm s}$ 3.1. Linear evolution of the fuel-lean H_2/air flames

⁹ Due to the unstable nature of the fuel-lean hydrogen/air flame, initial ¹⁰ perturbations imposed on the flame front grow exponentially in the linear ¹¹ stage. We first examine the dispersion relation in the preceding linear stage ¹² to better understand non-linear flame evolution. The numerical growth rate ¹³ is calculated based on the rate of perturbation amplitude A(t) [2, 15, 46], ¹⁴ i.e.,

$$\omega^* = \frac{1}{A(t)} \frac{\mathrm{d}A(t)}{\mathrm{d}t} = \frac{\mathrm{d}\ln[(A(t))]}{\mathrm{d}t} \tag{1}$$

As mentioned above, the growth rate and wavenumber are normalized by corresponding 1D unstretched planar flame parameters, the normalized growth rate ω and wavenumber k are

$$\omega = \omega^* \delta / S_L, k = k^* \delta = 2\pi \delta / h \tag{2}$$

The dispersion relation for lean premixed hydrogen flames at $T_0 = 100$ K and 300 K is shown in Fig. 2. To compare with results in the literature, data for the case at $\phi=0.5$ and $T_0 = 300$ K extracted from [24] are also plotted in Fig. 2. It is seen that results for $T_0 = 300$ K are close to the results in [24]. Considering the difference in chemical reaction mechanisms, good agreement is achieved between these results and the literature.

As shown in Fig. 2, the cryogenic condition significantly impacts flame instability development in the linear stage. The normalized growth rate ω increases greatly at cryogenic temperatures of $T_0 = 100$ K. The maximum normalized growth rate at $T_0 = 300$ K ($\omega = 1.2$) is much smaller than the maximum normalized growth rate at $T_0 = 100$ K ($\omega = 3.5$). As discussed in [15], a larger maximum growth rate implies stronger flame instability. Therefore, the flame instability is greatly enhanced at cryogenic temperatures. Note that the flame instability in the non-linear stage is relevant to the maximum growth rate in the linear stage [15, 31]. Therefore, the cryogenic temperatures are expected to affect the non-linear evolution of unstable flame. On the other hand, for each normalized wavenumber k smaller than the cut-off wavenumber at which the growth rate is zero, ω for $T_0 = 100$ K is always larger than that for $T_0 = 300$ K, indicating that perturbations in the range of unstable wavenumber grow faster at cryogenic temperatures.



Figure 2: Dispersion relation for premixed H_2/air flames at $\phi=0.5$, $T_0 = 100$ K and 300 K. The circles correspond to the numerical growth rate in this study. The solid curves are splines fitting these numerical growth rates according to Eq.(3). The black triangles refer to data extracted from [24]. Dashed lines are the theoretical growth rate of DLI. The dotted lines are the differences between the numerical and theoretical growth rates.

In the literature, the growth rate of lean flame is fitted by a fourth-order
polynomial [15, 47] in the form:

$$\omega_{fit} = \omega_{DL}k + \Pi_2 k^2 - \Pi_4 k^4 \tag{3}$$

where ω_{DL} is the expression of the theoretical growth rate of DLI [10, 11, 29]:

$$\omega_{DL} = \frac{1}{\sigma + 1} (\sqrt{\sigma^3 + \sigma^2 - \sigma} - \sigma) \tag{4}$$

It is noted that in Eq.(3), there is no constraint on the coefficient Π_2 , while the coefficient Π_4 must be positive to suppress the growth of short wavelength perturbations. The fitting coefficients according to Eq.(3) are listed in Table 2. To assess the individual effect of DLI, we also plot the ¹⁵ contribution of DLI for ambient and cryogenic flames based on Eq.(4), as ¹ denoted by the dashed lines in Fig. 2. It is seen that the growth rate of ² DLI, ω_{DL} , is larger at lower initial temperatures, indicating enhanced DLI at ³ cryogenic temperatures.

⁴ On the other hand, the differences between numerical growth rate and ⁵ theoretical growth rate are calculated and plotted in Fig. 2 to evaluate the ⁶ contribution of DTI, as shown by the dotted lines. It is found that the growth ⁷ rate due to DTI is also larger at lower initial temperatures. Additionally, ⁸ in Table 2 the coefficient Π_2 for $T_0 = 100$ K is much larger than that for ⁹ $T_0 = 300$ K. Since Π_2 is relevant to the effect of DTI, this also shows that ¹⁰ DTI is enhanced due to the cryogenic conditions. Therefore, at cryogenic ¹¹ temperatures, not only is DLI enhanced, but DTI is also enhanced.

Table 2: Comparison of fitting coefficients for $T_0 = 100$ K and 300 K.

case	ω_{DL}	Π_2	Π_4
$T_0 = 100 \text{ K}$	2.61	1.25	0.64
$T_0 = 300 \text{ K}$	1.18	0.31	0.27

Although this dispersion relation is derived from the linear stage of flame evolution, it provides a reasonable estimate for the instability in the nonlinear stage, as suggested by [15, 31]. Therefore, it is expected that in the non-linear stage, both DLI and DTI will also be greatly enhanced at cryogenic conditions for the fuel-lean premixed hydrogen/air flame.

17 3.2. Non-linear evolution of flame front propagation

The linear stage only lasts for a short interval. After a quick transi-18 tion, the unstable flame evolution changes from the linear to the non-linear 19 stage, characterized by complicated long-term dynamics of cellular structure 20 evolution, including cell splitting, cell merging, and lateral movement [29]. 21 Figure 3 shows the evolution of the lean flame ($\phi=0.5$) front in the channel 22 of $h = 10\delta$ for $T_0 = 100$ K and $T_0 = 300$ K. As flame instabilities develop, 23 the flame surface area increases, and the flame propagates towards the un-24 burnt gas on the left side. It is found that the perturbed sinusoidal flame 25 quickly transitions to the non-linear evolution stage with two cusps on the 26 front. During the flame propagation process, the shape of the flame front 27 changes occasionally. For $T_0 = 100$ K shown in Fig. 3(a), the depth of the 28

²⁹ two cusps is different after the planar flame changes to the two-cusp regime. ¹ The two-cusp flame front rapidly evolves to the single-cusp front at around ² $x/\delta=75$. Then, the flame propagates forwards in this single-cusp regime for ³ a long time with lateral movement. During this process, a double-cusp flame ⁴ front appears occasionally with a relatively short lifetime.

The evolution of the ambient flame at $T_0 = 300$ K is different. As shown 5 in Fig. 3(b), the flame shape changes from the two-cusp regime to the single-6 cusp regime at around $x/\delta=60$. This structure lasts a short interval, then 7 transitions to the two-cusp regime at around $x/\delta=58$. However, this regime 8 is unstable, and it reverts to the single-cusp regime. Finally, the flame moves 9 towards the inlet in a single-cusp regime. The comparison between $T_0 =$ 10 100 K and $T_0 = 300$ K demonstrates that the lateral movement is more 11 pronounced, and the cusp is deeper for the cryogenic flame, which is thereby 12 more unstable. 13



Figure 3: Temporal evolution of flame front propagating in a channel with $h = 10\delta$ for (a) $T_0 = 100$ K, $\phi=0.5$, (b) $T_0 = 300$ K, $\phi=0.5$. The flame propagates from the right to the left.

The flame front evolution for the stoichiometric case ($\phi=1$) is shown in 14 Fig. 4. It is noted that for the hydrogen/air mixture at $\phi=1$, the effective 15 Lewis number is slightly larger than unity, i.e., $Le_{eff} > 1$. Therefore, the 16 flame is diffusional-thermally stable, and the primary factor affecting flame 17 front evolution is DLI. It is seen that without DTI, the non-linear evolution of 18 the hydrogen/air flame exhibits a relatively simple structure at both ambient 19 and cryogenic temperatures. The flame propagates to the left side in a stable 20 single-cusp regime without cell splitting or merging processes. In addition, 21 the position of the single cusp on the flame front is almost the same at differ-22 ent instants, i.e., the cusp stays at around $y/\delta=7$ without lateral movement. 23 This indicates that DLI plays a limited role in the non-linear evolution of the 24

flame front. Combined with previous lean flame results, dynamics of nonlinear evolution, including cell splitting, cell merging, and lateral movement,
are more associated with the DTI.

³ Nevertheless, the intensity of flame instability is different for $T_0 = 100$ K ⁴ and $T_0 = 300$ K. Comparison between Figs. 4(a) and (b) shows that the ⁵ normalized cell depth is larger at a cryogenic temperature of $T_0 = 100$ K. ⁶ This demonstrates that DLI is enhanced at cryogenic temperatures in the ⁷ non-linear stage.



Figure 4: Temporal evolution of flame front propagating in a channel with $h = 10\delta$ for (a) $T_0 = 100$ K, $\phi=1$, (b) $T_0 = 300$ K, $\phi=1$. The flame propagates from the right to the left.

Simulations were also performed on the fuel-rich hydrogen/air mixture with $\phi=2.5$. The flame evolution in the non-linear stage is similar to the stoichiometric case shown in Fig. 4. The results for $\phi=2.5$ are not shown here to avoid duplication. The primary difference between ambient and cryogenic flames is the normalized cusp depth, which is larger for $T_0 = 100$ K, indicating stronger DLI at lower temperatures.

As mentioned above, the channel width may significantly affect the flame 14 evolution. To study this effect, Fig. 5 shows the fuel-lean cryogenic flame 15 $(T_0 = 100 \text{ K}, \phi = 0.5)$ propagation in channels with different widths. Note 16 that the evolution of the flame front for $h = 10\delta$ is shown in Fig. 3 and is 17 not repeated in Fig. 5 to avoid redundancy. As the channel width increases 18 from $h = 4\delta$ to $h = 10\delta$, the non-linear evolution of the flame front exhibits 19 distinguishing regimes: For $h = 4\delta$, the regime is a stable single-cusp flame 20 front, with one small cusp located at around $y/\delta=3$. For $h=5\delta$, the flame 21 front is a single-cusp regime with lateral movement. When the channel width 22 increases to $h = 6\delta$, the flame regime changes again: the flame propagates 23 towards the unburned gas in a complex regime, in which single-cusp and two-24 cusp alternately appear on the flame front. By further increasing to $h = 8\delta$, 25

the flame regime is a stable double-cusp regime in which two cusps on the 26 flame front with a fixed position at $y/\delta=2$ and $y/\delta=6$. Interestingly, the flame 1 front shape for $h = 8\delta$ seems to be mirrored from that for $h = 4\delta$. The quasi-2 steady propagation regime (stable single-cusp and double-cusp) observed in 3 cases with $h = 4\delta$ and 8δ may be related to the critical wavenumber (k_m) associated with the maximum normalized growth rate. According to the 5 results in Fig. 2, $k_m \approx 1.32$, corresponding to a critical wavelength of $\lambda_m \approx$ 6 4.7δ . The channel widths for the quasi-steady propagation regime are close 7 to, but slightly smaller than, the integer multiples of λ_m . This observation is 8 also consistent with the results in the previous study [24]. When the channel g width is $h = 10\delta$, as shown in Fig. 3(a), the flame propagation regime is 10 alternative single-cusp and double-cusp. Therefore, the non-linear evolution 11 of the flame front is very sensitive to the change in channel width. 12



Figure 5: Temporal evolution of fuel-lean cryogenic flame ($T_0 = 100$ K and $\phi = 0.5$.) front propagating in channels with different widths: (a) $h = 4\delta$, (b) $h = 5\delta$, (c) $h = 6\delta$, and (d) $h = 8\delta$. The flame propagates from the right to the left.

Previous studies [30, 36, 48] have shown that the channel width strongly influences the flame structure. The "flame finger" structure [36] cannot be observed when the channel width is too small. It is found that the channel width larger than 25δ is proper for the evolution of flame finger structure. As shown in Fig. 6(a), one flame finger structure can be observed for $h = 20\delta$. Moreover, the flame finger is smooth, and small wrinkles do not appear on the flame branches that compose the flame finger structure. When the channel



Figure 6: Temporal evolution of flame front propagating in channels with different widths (a) $h = 20\delta$, (b) $h = 40\delta$, and (c) $h = 100\delta$ for $T_0 = 100$ K and $\phi=0.5$. The flame propagates from the right to the left.

width increases to $h = 40\delta$, as shown in Fig. 6(b), a flame finger structure with small wrinkles superimposed on its branches is observed. This structure exhibits distinct lateral movement. In addition, isolated flame pockets can be observed in the late stage due to the collision of wrinkled flame segments. The results for $h = 100\delta$ are shown in Fig. 6(c). After transitioning to the non-linear stage, small flame finger structures with lateral movement can
merge into a large flame finger. There are many small wrinkles with different
length scales on the branches of the flame finger. The flame front is wrinkled
and accelerated as it propagates towards the unburnt gas.



Figure 7: Contours of normalized temperature (T_{norm}) for (a) $T_0 = 100$ K at t = 20.8 and (b) $T_0 = 300$ K at t = 92. The channel width is $h = 100\delta$.

The contours of normalized temperature $(T_{norm} = (T - T_0)/(T_b - T_0))$ at 4 the instant when a cellular structure is fully developed are shown in Fig. 7. It 5 is seen that the cryogenic flame front is more wrinkled compared to the am-6 bient flame. In addition, the intense wrinkling of the cryogenic flame forms 7 a deep channel containing unburnt gas between large flame finger structures. 8 The subsequent combustion of the unburnt gas within the deep channel pro-9 duces a sharp reduction in the flame surface area. As a result, the surface 10 area of the cryogenic flame can vary significantly during propagation. Con-11 sistent with previous study [49], super-adiabatic temperature phenomena are 12 observed for both fuel-lean flames, with $T_{norm,max} = 1.1$ for $T_0 = 100$ K and 13 $T_{norm,max} = 1.05$ for $T_0 = 300$ K. Since the super-adiabatic temperature 14 phenomena are associated with the imbalance between thermal and species 15 diffusion, the larger super-adiabatic temperature at cryogenic conditions in-16 dicates that DTI is more pronounced at lower temperatures. 17

It is clear that the alternating appearance of single-cusp and double-cusp flame fronts and the evolution of flame finger structures in fuel-lean premixed hydrogen/air flames are closely related to long-term dynamics, including cell ²¹ splitting, cell merging, and lateral movement [29]. To better understand the ¹ flame evolution, their mechanisms are analyzed in the following subsection.

² 3.3. Long-term flame dynamics

To investigate the mechanism for cellular structure splitting and merging, 3 the evolution of the heat release rate (HRR) contour and the corresponding 4 flow field near the flame front is considered for the fuel-lean cryogenic case $(T_0 = 100 \text{ K}, \phi = 0.5, h = 10\delta)$. The flame front is defined as the iso-contour 6 line of the mass fraction of H_2O , which corresponds to the maximum tempera-7 ture gradient of the 1D unstretched planar flame. Streamlines near the flame 8 front are superimposed on the HRR contour to interpret the cell splitting 9 and merging process in Figs. 8(1a-1c) and 8(2a-2c), respectively. Figure 9 10 shows the profiles of flow speed in the x direction U_x , local heat release rate q, 11 density-weighted displacement speed S_d^* , stretch rate K along the flame front 12 and the flame front position x as functions of y for several instants during 13 the cell splitting and merging processes. It is noted that in Figs. 9(1e) and 14 (2e) the flow direction in the unburnt region is from bottom to top and all 15 parameters except q are normalized. 16

The splitting process of cellular structure is relevant to the interactions 17 between the flame stretch, local reactivity, and flow. In Fig. 8(1a) at t=56.4, 18 the flame cell is relatively smooth, and a large cusp is located at around 19 $y/\delta=2$. A streamline focusing phenomenon is observed near the cusp. As 20 shown in Fig. 9(1a), the unburnt gas speed ahead of the cusp is larger than 21 that near the convex segment of the cell. This is a feature of DLI due to 22 the interaction between the flame front and the flow near it [11, 20]. Gas 23 expansion across the flame front induces flow acceleration, which enhances 24 the flame front wrinkling and leads to a deeper cusp. In the middle of the 25 large cell at around $y/\delta=8$, the flame stretch rate becomes negative, and 26 the HRR is relatively small compared with the two flame branches near it, 27 which can be seen in Figs. 9(1b) and (1d) at t=56.4. Therefore, a small 28 concave segment towards the unburnt gas is formed, indicating the birth of 29 a new cusp. As this concave segment evolves in the flow, its depth increases 30 due to the interaction between flow and flame front, as shown in Figs. 8(1b)31 and 9(1a-1e). This process is relevant to the development of DLI. There-32 fore, the streamline focusing phenomenon becomes significant near the new 33 cusp at around $y/\delta = 8$. In Figs. 8(1c) and 9(1e), this new cusp forms with 34 considerable depth. Note that the interaction between flame stretch and 35 chemistry also plays an important role in the cell splitting process since the 36

³⁷ cusp deepening process is accompanied by a change in curvature and flame
¹ stretch rate that affects the chemical reaction through Lewis number effect,
² as shown in Figs. 9(1b) and (1d). In summary, the complex interactions
³ between flow, flame stretch, and chemistry lead to the splitting of flame cells
⁴ and the formation of a new cusp on the flame front.



Figure 8: Evolution of heat release rate contour superimposed by streamlines near the occurrence of cell splitting (1a-1c) and cell merging event (2a-2c) for $T_0 = 100$ K and $\phi=0.5$. The channel width is $h = 10\delta$.

The cell merging process is shown in Figs. 8(2a-2c) and 9(2a-2e). Note 5 that a periodic boundary condition is imposed in the y direction. At t=58.56 in Figs. 8(2a) and 9(1e), the flame front consists of two convex cells with 7 different length-scales: a large cell within the range of $2.5 \le y/\delta \le 10$ and 8 a small cell within $0 \le y/\delta \le 2.5$. These two cells are connected by two 9 cusps between them. Since the HRR on the larger cell is not uniform, the 10 propagation speed is different along the flame front of the large cell. Specif-11 ically, the HRR is larger on two branches of the large cell near the cusps 12 and smaller in the middle of the cell. This can be observed in Figs. 8(2a-2c)13 and 9(2b). Therefore, the large cell tends to expand in the lateral direction 14 (y direction), which narrows the channel ahead of the small cell, as shown 15 in Figs. 8(2b) and 9(2a-2e). Flow focusing also contributes to the increase 16 in cusp depth. The narrow channel ahead of the small cell acts like a 'cusp', 17 and therefore, the flow speed in the 'cusp' $(0 \le y/\delta \le 2.5)$ increases as the 18



Figure 9: Temporal evolution of profiles for flow speed, U_x , heat release rate, q, densityweighted displacement speed, S_d^* , stretch rate, K, and the flame front position, x, along the flame front during cell splitting (1a-1e) and cell merging process (2a-2e).

large cell expands, as shown in Figs. 8(2b) and 9(2a). Due to the increased 19 flow speed, the small flame cell cannot propagate towards the unburnt gas 1 on the left. Gradually, it is pushed back by the strong flow. As a result, the 2 small cell becomes flat (see Fig. 9(2e)). Since the differential diffusion effect 3 is strong for this negatively stretched flame segment (see in Fig. 9(2d)), the 4 HRR of the smaller cell also decreases gradually during this process, which can be seen in Fig. 9(2b). Finally, as shown in Fig. 8(2c), the small cell 6 disappears, implying the completion of the cell merging process. Therefore, 7 the cell merging is also associated with the interaction between flow, flame 8 stretch, and chemical reactions. 9

In addition, Fig. 9(1b) also explains the mechanism for the lateral movement of cusps. At t=56.9 (green line), there is a manifest difference in heat release rate between the two flame branches forming the cusp at $y/\delta=2$. Affected by this, the flame propagation speeds are also different. Therefore, the strong flame branch near $y/\delta=1$ pushes the weak flame branch near $y/\delta=3$, leading to the lateral movement of the cusp towards the y-axis direction. Therefore, the cusp moves to the right from t=56.9 to t=57.1 (black line), which can be seen from Fig. 9(1e). As mentioned above, the HRR distribution is affected by the cell splitting and merging processes. Therefore, lateral movement is frequently observed for flames in the regime of alternative appearance of single-cusp and double-cusp, as can be observed in Figs. 3, 5(b), 5(c) and 6.

In summary, strong interaction among flow, flame stretch, and chemical
reactions (heat release) plays a primary role in the cell splitting and merging
processes. Therefore, the mechanisms of the chaotic evolution of the fuel-lean
flame front are relevant to the 'flow-stretch-chemistry' interaction.

12 3.4. Cellular flame structure

In order to interpret the effect of cryogenic temperatures on the local flame structure, the joint distribution of progress variable (PV) and the normalized reaction rate of hydrogen are analyzed. The progress variable is defined as

$$PV(Y(\mathbf{H}_2)) = 1 - \frac{Y(\mathbf{H}_2) - Y_b(\mathbf{H}_2)}{Y_u(\mathbf{H}_2) - Y_b(\mathbf{H}_2)}$$
(5)

where $Y(H_2)$ is the mass fraction of H_2 , $Y_u(H_2)$ and $Y_b(H_2)$ are the mass fraction of H_2 in the unburnt and burned gas, respectively.

The joint distribution, conditional average and 1D unstretched planar 18 flame solution of progress variable and corresponding source term for case 19 $h = 10\delta$ are shown in Fig. 10. It is seen that for the fuel-lean flames, the 20 conditional average of source term is much higher than the 1D unstretched 21 flame solution. On the other hand, in Fig. 10(c), the cryogenic flame at $\phi=1$, 22 the conditional average of source term is close to the 1D unstretched planar 23 flame solution, indicating that the effects of DLI on local flame structure 24 and the enhancement in reaction rate are negligible. Comparison in Fig. 10 25 demonstrates that DTI of fuel-lean flames has a significant impact on the lo-26 cal reaction rate enhancement. Therefore, DLI accelerates flame propagation 27 mainly through the increase in the flame surface area, while DTI can lead to 28 flame acceleration through both an increase in the flame surface area and lo-29 cal reaction rate enhancement. Furthermore, compared to the ambient flame 30 at $T_0 = 300$ K and $\phi = 0.5$, the cryogenic flame at $\phi = 0.5$ exhibits a larger 31 normalized conditional average of the source term, which demonstrates that 32

at a lower temperature, the DTI has a stronger influence on local reaction
rate enhancement.

To assess the effect of channel width on flame propagation, the joint distribution of the progress variable and the corresponding source term for $h = 100\delta$ is shown in Fig. 11. It is seen that the normalized conditional averages of the source term do not change significantly from cases $h = 10\delta$ shown in Fig. 10. Therefore, increasing the channel width from $h = 10\delta$ to $h = 100\delta$ has a limited effect on the local reaction rate enhancement for the fuel-lean flames considered in this work.

⁹ 3.5. Flame acceleration

Strong DLI and DTI can greatly enhance the flame front wrinkling, accelerating flame propagation. An approximate measure of the flame speed for the wrinkled flame is consumption speed, S_c , defined as in [31],

$$S_c = \frac{1}{\rho_u(Y_u(\mathbf{H}_2) - Y(\mathbf{H}_2)) \cdot A_0} \int \dot{\omega} dx dy \tag{6}$$

¹³ where $\dot{\omega}$ is the net consumption rate of H₂, ρ_u the unburned gas density, ¹⁴ $Y_u(\text{H}_2)$ the mass fraction of H₂ in the unburned gas, A_0 the flame surface ¹⁵ area at t=0, i.e., $A_0 = h$. Generally, flame instabilities can affect overall ¹⁶ flame speed through two mechanisms: flame surface area increase due to ¹⁷ flame wrinkling and local flame speed change related to flame stretch [36, 50]. ¹⁸ To quantify their individual effect, S_c is decomposed into the production of ¹⁹ flame surface area increase A/A_0 and stretch factor I,

$$S_c/S_L = I \cdot (A/A_0) \tag{7}$$

where A is the surface area of the wrinkled flame front. It is noted that the 20 fuel-lean flame surface is defined as the iso-contour line of $PV(Y(H_2))=0.9$ [49]. 21 This definition leads to reasonable results for the flame surface area, espe-22 cially for the fuel-lean flame, which is prone to strong DTI. For stoichiometric 23 or fuel-rich cases, the iso-contour line of water mass fraction $(Y(H_2O))$ corre-24 sponding to the maximum temperature gradient of the 1D unstretched planar 25 flame is selected to the calculated flame surface area, as the differential dif-26 fusion effect could lead to locally fuel-rich mixture [31]. The stretch factor 27 measures the effect of local reactivity on the consumption speed. If I > 1, 28 the effect of flame stretch enhances the consumption of fuel (local reaction 29 rates) and vice versa. 30



Figure 10: Joint distribution, conditional average (red line) and 1D unstretched flame solution (grey line) of the progress variable $PV(Y(H_2))$ and the normalized source term of $PV(Y(H_2))$ for (a) $T_0 = 100$ K, $\phi=0.5$, (b) $T_0 = 300$ K, $\phi=0.5$, and (c) $T_0 = 100$ K, $\phi=1$. The channel width is $h = 10\delta$.



Figure 11: Joint distribution, conditional average (red line) and 1D unstretched flame solution (grey line) of the progress variable $PV(Y(H_2))$ and the normalized source term of $PV(Y(H_2))$ for (a) $T_0 = 100$ K, $\phi=0.5$ and (b) $T_0 = 300$ K, $\phi=0.5$. The channel width is $h = 100\delta$.



Figure 12: Evolution of the normalized consumption speed S_c/S_L , flame surface area increase A/A_0 and stretch factor I for case $T_0 = 100$ K and $\phi = 0.5$, $h = 10\delta$.

The effect of equivalence ratio and cryogenic temperatures on flame evo-31 lution for $h = 10\delta$ is shown in Fig.12. It is found that the consumption speed 1 oscillation is only observed for $\phi = 0.5$ with strong DTI. This result is rea-2 sonable since the chaotic evolution of cellular structure originates from DTI. 3 On the other hand, the acceleration of fuel-lean cryogenic flame is the most 4 pronounced, highlighting that the combined effects of both DLI and DTI 5 have a significant influence on flame acceleration. Further analyses shown in 6 Figs. 12(b) and (c) demonstrate that the acceleration results from enhancement in both A/A_0 and I. The primary contribution is from the increase in 8 I. This shows that DTI is the dominant factor in fuel-lean flame acceleration, 9 consistent with the previous study [36]. In addition, pure DLI also leads to 10 intense flame acceleration, which can be seen in the cryogenic and ambient 11 cases at $\phi = 1$. For fuel-rich flames, flame acceleration is greatly suppressed, 12 with S_c/S_L close to 1. It is clear that for $\phi \ge 1$, the acceleration is purely 13 caused by an increase in A/A_0 . The local reaction rate is not enhanced by 14 DLI, which is consistent with the results shown in Fig. 10(c). 15



Figure 13: Evolution of the normalized consumption speed S_c/S_L , flame surface area increase A/A_0 and stretch factor I for case $T_0 = 100$ K and $\phi = 0.5$ in domain with different widths h.

Figure 13 shows the effect of channel width $(h \leq 10\delta)$ on the flame

acceleration in the fuel-lean mixture at $T_0 = 100$ K. The flame speed changes 17 periodically due to chaotic cell evolution. The time period of oscillations is 1 affected by both the channel width and the lateral movement speed. However, 2 the lateral movement speed is complex and can be affected by many factors, 3 such as the nonlinear behavior of the flame front, the Lewis number and the 4 temperature distribution along the flame front [51]. Deriving an analytical 5 expression for the oscillation period is beyond the scope of this work and 6 warrants further investigation. In addition, the flame speed enhancement, S_c/S_L , is larger than 1.5 for all channel widths considered. Both A/A_0 and I 8 contribute to the flame acceleration. Moreover, Fig. 13 shows that the stretch 9 factor I oscillates around I = 2.0 with a lower bound of I > 1.5, while A/A_0 10 fluctuates around $A/A_0 = 1.2$ with an upper bound of $A/A_0 < 1.5$. Since I 11 is only relevant to the DTI and the DTI also contributes to A/A_0 , it can be 12 concluded that the DTI plays a dominant role in fuel-lean flame propagation. 13 Previous studies [36, 50] have shown that DLI can enhance the development 14 of DTI. Therefore, DLI may also play a role in flame acceleration through 15 a direct mechanism of increasing flame surface area or through an indirect 16 mechanism of promoting DTI. It is worth noting that the dependence of 17 S_c/S_L , A/A_0 and I on h is sensitive, which is caused by the chaotic evolution 18 of the flame front under strong DTI and DLI. Therefore, channel width has a 19 significant effect on flame evolution regimes and thereby flame acceleration, 20 especially for narrow channels. 21

Table 3: The mean values of normalized consumption speed S_c/S_L , flame surface area increase A/A_0 , and stretch factor I for fuel-lean hydrogen/air flame at $T_0 = 100$ K and 300 K. The channel width is $h = 100\delta$.

case	S_c/S_L	A/A_0	Ι
$T_0 = 100 \text{ K}$	4.25	1.95	2.17
$T_0 = 300 \text{ K}$	2.04	1.40	1.45

As mentioned above, a large domain is necessary to obtain geometryindependent results. For flame propagation in wide channels, the results are shown in Fig. 14. Based on the data after the cellular structure is fully developed in the wide channel of $h = 100\delta$, the domain-independent mean values of S_c/S_L , A/A_0 , and I for fuel-lean hydrogen/air flames at $T_0 = 100$ K and 300 K are calculated and listed in Table 3. Compared to $T_0 = 300$ K, the larger S_c/S_L at $T_0 = 100$ K results from the increase in both A/A_0 and I,



Figure 14: Evolution of the normalized consumption speed S_c/S_L , flame surface area increase A/A_0 and stretch factor I for $\phi=0.5$ in domain with different widths and initial temperatures.

which demonstrates that both DLI and DTI are enhanced under cryogenic conditions. Since the values of I are larger than A/A_0 , the DTI has a greater contribution to the flame acceleration than the DLI. It is noted that the mean values in Table 3 for the cryogenic flame are calculated during the later stage of flame propagation, when most of the flame segments are contained within the computational domain. A small portion of flame segments extending beyond the domain may lead to slightly underestimated mean values; however, this does not affect the main conclusions.

Comparison between Figs. 13 and 14 shows that the periodic oscillation 8 phenomena disappear when the channel width is large. Only small spikes 9 appear on the evolution of consumption speed in Fig. 14. This is reasonable 10 since the cellular flame front evolution is more violent without the confine-11 ment of channel width. Additionally, the large oscillations observed in Fig. 12 14 are relevant to the flame segments extending beyond the computational 13 domain, which causes a pronounced reduction in flame surface area and flame 14 consumption speed. Compared to small channels shown in Fig. 13, the value 15 of A/A_0 for a cryogenic flame increases to around $A/A_0 \approx 1.95$, while the 16 stretch factor I does not increase significantly. Therefore, a small channel 17 width can suppress the development of flame instabilities through the flame 18

¹⁹ surface area, resulting in weaker flame acceleration. On the other hand, the ¹ stretch factor I is less sensitive to the channel width, which agrees well with ² the analysis in the previous section.

An interesting observation is the large value of $S_c/S_L \approx 6$ for $h = 40\delta$ in Fig. 14(a) and 14(b) shows that this large value is associated with an increase in flame surface area, resulting from the formation of a very deep cusp during the flame propagation, as shown in Fig. 6(b). Compared to the case with $h = 100\delta$, a smaller channel width of $h = 40\delta$ enhances the flame acceleration. Therefore, a smaller channel width does not always suppress the flame wrinkling and flame acceleration. This also indicates that channel width has a great impact on cellular flame evolution and acceleration.

11 4. Conclusions

The evolution and acceleration of fuel-lean hydrogen/air flames at ambi-12 ent and cryogenic temperatures (300 K and 100 K) are studied by a series 13 of two-dimensional simulations incorporating detailed chemistry and trans-14 port models. The analysis reveals that cryogenic temperatures significantly 15 enhance both Darrieus-Landau instability (DLI) and diffusional-thermal in-16 stability (DLI) of fuel-lean hydrogen/air flames. In the linear stage, the 17 growth rates of both DLI and DTI are found to increase significantly at 18 cryogenic temperatures. The non-linear stage of cellular flame evolution ex-19 hibits chaotic characteristics influenced by unburned gas temperature and 20 channel width, with DTI emerging as the primary driver of this chaotic evolu-21 tion. Long-term dynamics of cellular structures, including cell splitting, cell 22 merging, and lateral movement, are observed and interpreted for fuel-lean 23 hydrogen/air flames. It is found that cell splitting and merging are mainly 24 caused by the flow-stretch-chemistry interaction. The unbalanced heat re-25 lease rate on two branches of the cusp can induce the lateral movement of 26 cusps. In the absence of DTI, the flame propagates in a single-cusp regime 27 without cell splitting, merging, or lateral movement due to a relatively weak 28 stretch-chemistry interaction. 20

Flame structure analysis reveals a significant enhancement of local reaction rates in lean hydrogen/air flames under cryogenic conditions. For diffusive-thermally stable hydrogen/air flames with $\phi = 1$, the cryogenic temperature has a negligible effect on the local reaction rate. The pronounced acceleration of fuel-lean cryogenic flames stems from the simultaneous enhancement of flame surface area and stretch factor, reflecting the combined ³⁶ influence of DLI and DTI. While both instabilities contribute to flame ac-¹ celeration, DTI emerges as the dominant mechanism, with DLI providing ² secondary enhancement. The flame evolution demonstrates particular sensi-³ tivity to channel geometry when the width $h < 10\delta$: minor width variations ⁴ can substantially alter the evolution of flame consumption speed. Further ⁵ analysis indicates that channel width influences flame behavior primarily by ⁶ constraining the flame surface area, while local reaction rates remain largely ⁷ independent of geometric constraints.

In this study, the Soret diffusion is not considered. In previous study [52], 8 the Soret diffusion effect was examined at elevated temperatures. It would 9 be interesting to quantify the influence of the Soret diffusion at cryogenic 10 temperatures in future studies. Our study employs two-dimensional simula-11 tions, which capture important aspects of flame dynamics but have inherent 12 limitations. In real-world applications, flames propagate three-dimensionally, 13 potentially exhibiting additional instability mechanisms that could enhance 14 flame front wrinkling and acceleration beyond what we observe in two di-15 mensions. Introducing the third dimension may reveal new patterns of flame 16 evolution and more complex interactions between DLI and DTI. Future in-17 vestigations using three-dimensional simulations in large computational do-18 mains would complement our current findings and provide a more complete 19 understanding of flame behavior under cryogenic conditions. 20

21 5. Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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